

Renewable Energy Podcasts



Stephen Lacey



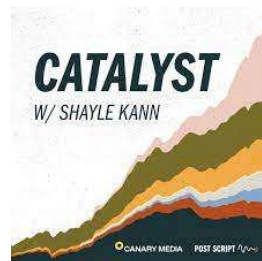
Irish / French



English



Shayle Kann



Australians

- Question #

1

Difficulties
Physical feasibility
Science behind-2
The underlying physics behind engineering designs
Compare fundamental science between different approaches
Viability of sustainable projects
Detailed equations behind sustainable energy
Development of solutions

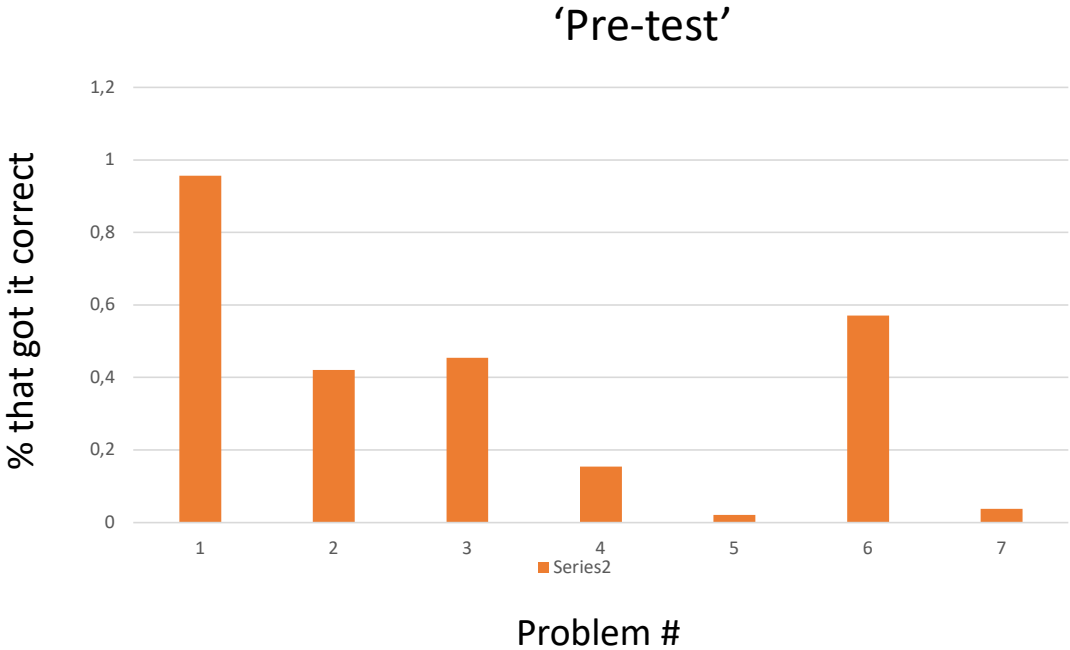
Question #3

Lecture	Reading	Exercises
8,13	6,74	8,70
1,26	1,70	1,33

- Question #

2

Storage-5
New startups
Conversion-2
Nuclear-5
Batteries-1
Wind Power - 7
Electrochemistry-2
H2 Storage
Electrolysis-2
CO2 capture-4
Power2X-
Photosynthesis
Solar-9



Photovoltaics



Lecture - Learning Objectives

At the end of this lecture you should:

- Understand the detailed balance for solar cells, and why maximum efficiency for a single photoabsorber is 33%
- Be able to analyze the basic principles of photovoltage and factors that can effect it
- Understand how p-n junctions work and their relation to solar cells.

How much energy can we get ?

- Comparison of renewable energy sources:
 - Geothermal: 0.3-2 TW
 - Hydro Power: 3-4 TW
 - Biomass: 2-6 TW
 - Wind Power: 25-70 TW
 - Solar Power: 123,000 TW
- Solar will always provide us with enough energy to power the planet.
- *The real question is can we do it cheap enough to be economically viable.*

Extremely Wrong



Secretary Chris Wright   @SecretaryWright · 5h

Even if you wrapped the entire planet in a solar panel, you would only be producing 20% of global energy.

One of the biggest mistakes politicians can make is equating the ELECTRICITY with ENERGY!



Readers added context

Earth gets ~1.5M TWh/day of solar energy—over 3,000× global energy use (~165K TWh/year). Covering just 1% of land with panels could—theoretically—power the planet. Electricity is energy, and electrification replaces fossil use in transport, heat, and industry.

8:28 PM · Sep 2, 2025



1.1K



Reply



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Ambitious PV system goals

Ambition: Cost effective grid power from PV **2012**

July 2024

Requirements:

Utility system costs: $C_s \sim 1$ \$/W

Currently ~ 3.5 \$/W

1.00 \$/W

Reliability: ~ 30 yrs

Efficiency: $\eta \geq 25\%$ (!)

Electricity cost: $\propto C_s / \eta$

Materials: Earth abundant, preferably non-toxic, recyclable

Module cost: ~ 0.5 \$/W

Currently ~ 1.7 \$/W

0.085 \$/W

Cell cost: ~ 0.25 \$/W

Currently ~ 1 \$/W

0.032 \$/W

+ affordable energy storage



PV cell



PV module



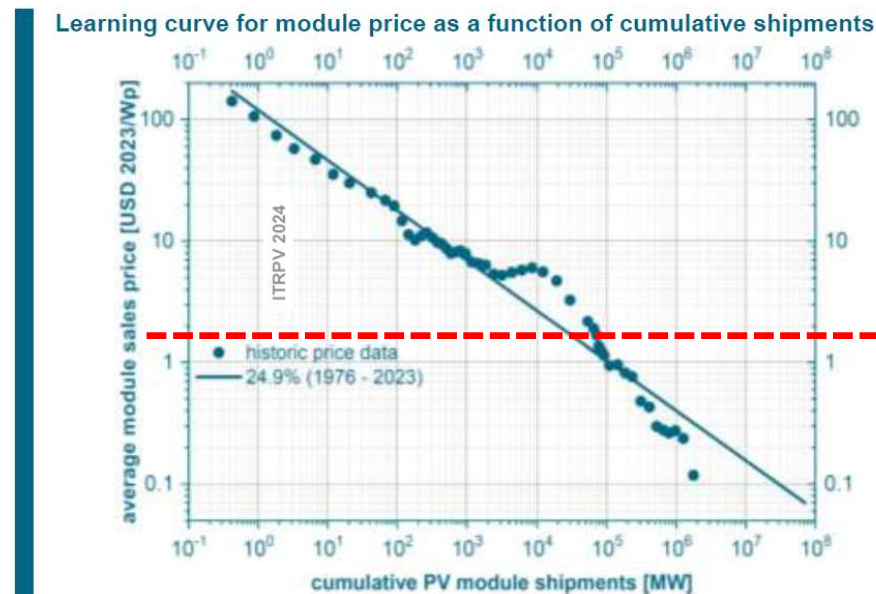
PV system (Nellis Air Base, US)

Data from
PVinsights.com &
SEIA.org

Solar Cell Costs

- Record solar price: 2020: 10.4 \$/MWh (Saudi Arabia)
2022: -4.5 \$/MWh (Portugal)- Deal also includes storage.

- Avg. residential electricity cost in EU: 250 \$/MWh
- The top ~10 biggest companies for Si solar cells all are from China.



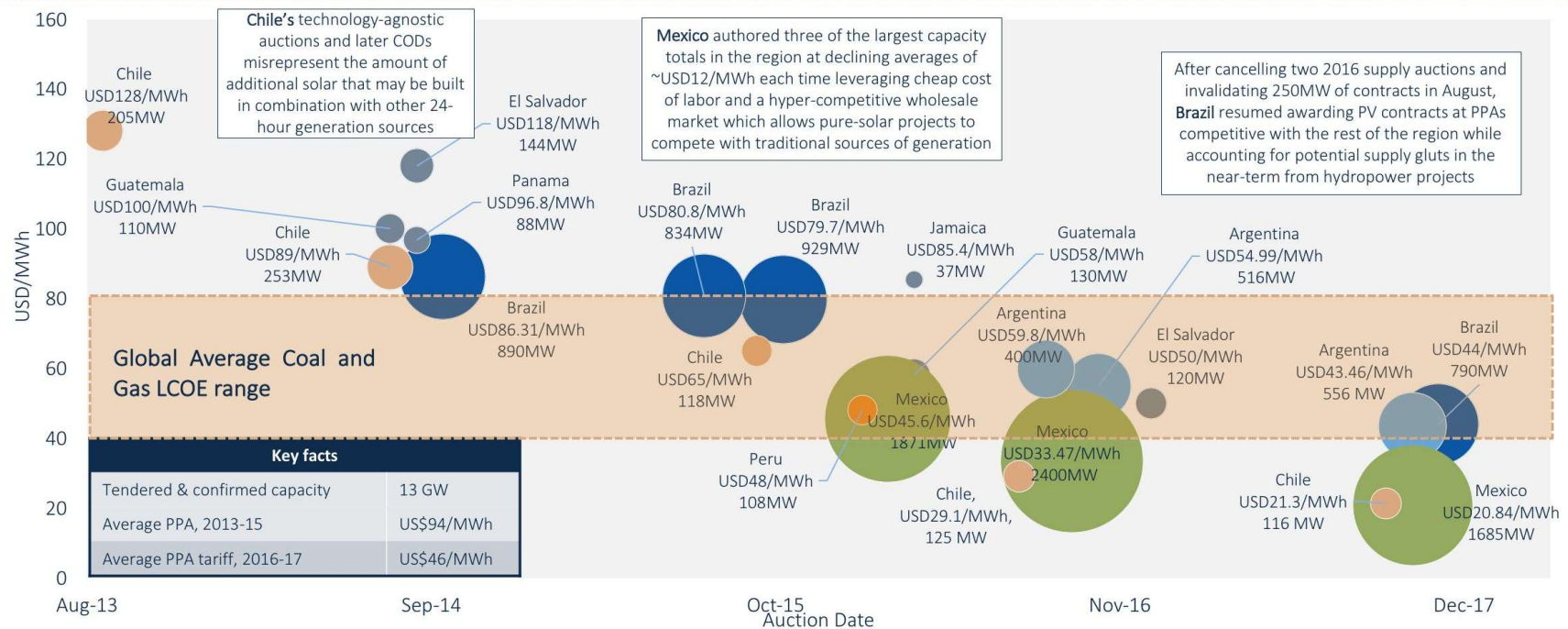
Reference: ITRPV Report 15th Edition

Fig.1: Learning curve for module spot market price as a function of cumulative PV module shipments.

Reverse Auction

- Countries say they want a given amount of renewable electricity (with conditions) and then the lowest bid gets the job.
- This has been an absolute success. Prices have dropped incredibly due to this.

Latin America & Caribbean Tendered Projects by Bid Price and Capacity, 2013-2017

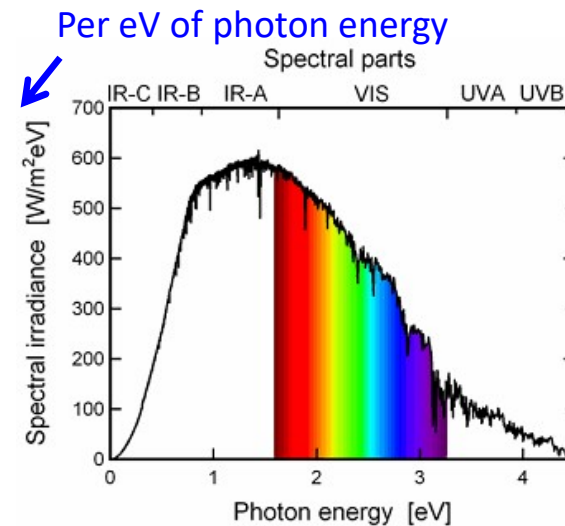
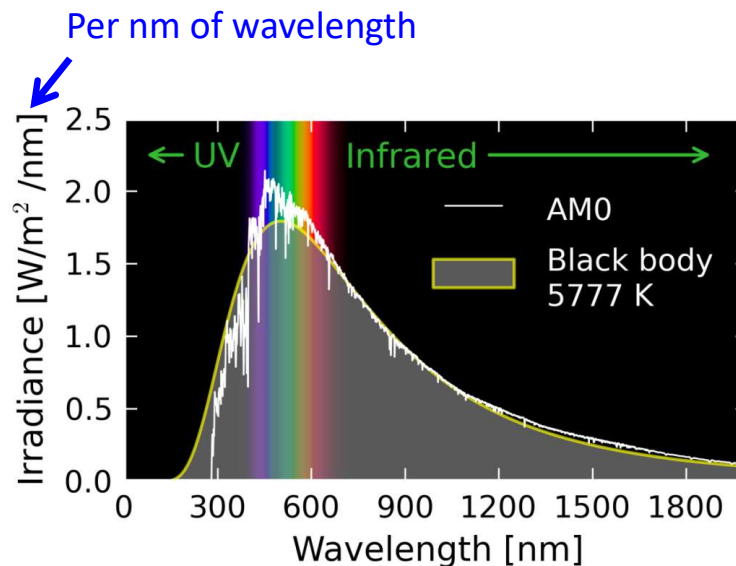


Source: GTM Research Global Solar Demand Monitor Q4 2017

Incoming light– quick review

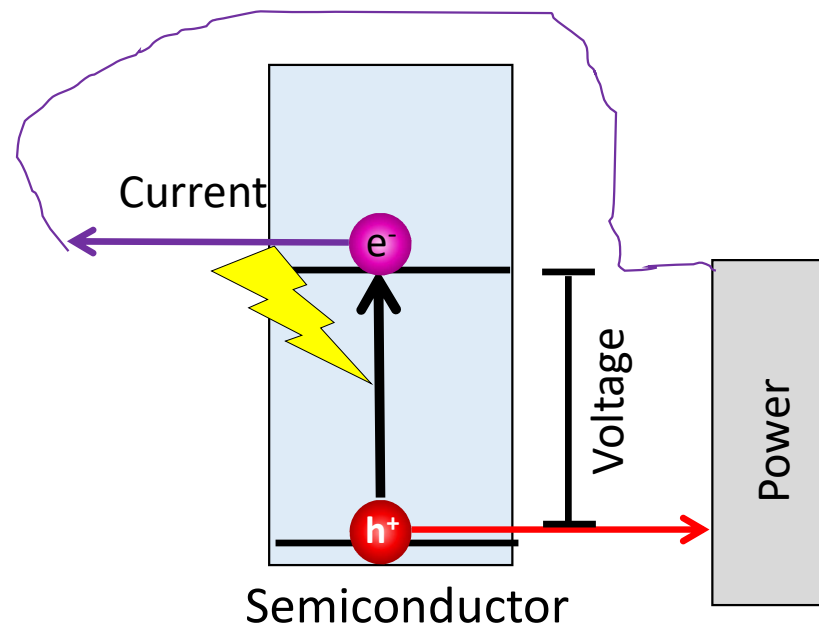
- While typically the plots are irradiance vs. wavelength, irradiance vs. photon energy can also be useful.
- We can convert these graphs using the following equation:

$$E(eV) = \frac{1240}{\lambda(nm)}$$



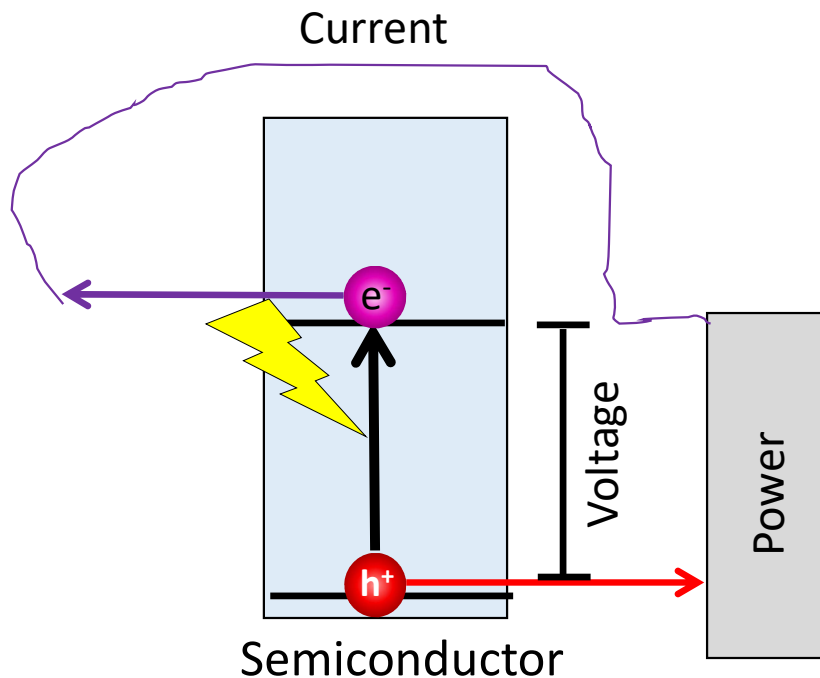
Solar cells – quick review

- From a first order theory we should be able to get power according to the voltage and current

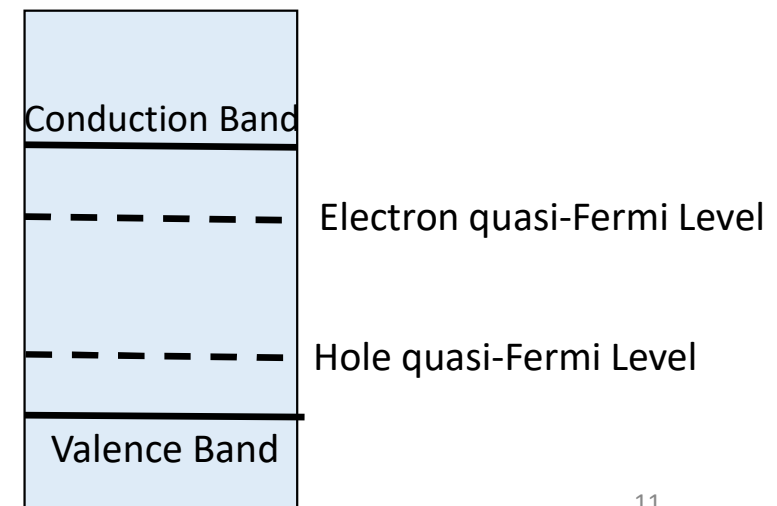


Solar cells – more detailed description

- From a first order theory we should be able to get power according to the voltage and current



- From a more in-depth approach it is actually the splitting of our Fermi level that gives us photovoltage.



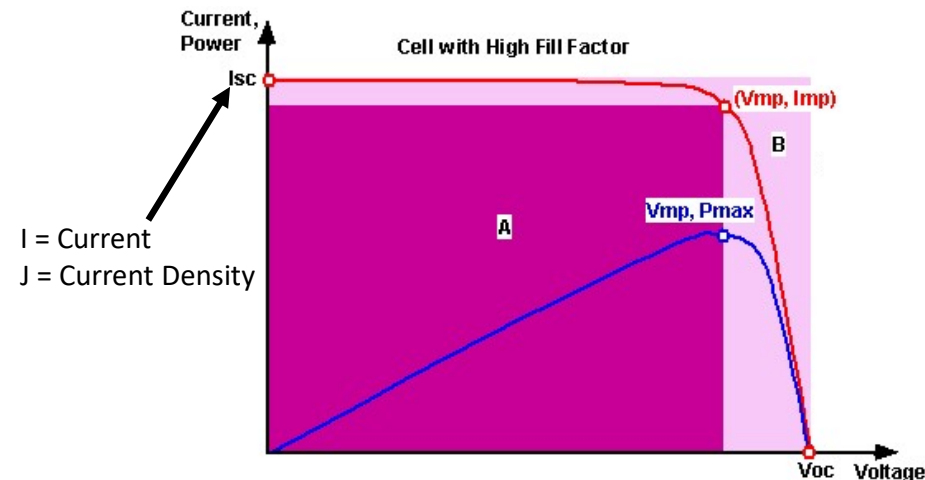
Relating voltage to current

- We want power (or power density) from our solar cell and this is simply:

$$P = V \times j$$

where V is voltage and j is current density.

- Increasing our current decreases our voltage, leading to a j-V curve as shown below



$$FF = \frac{I_{mp} V_{mp}}{J_{sc} V_{oc}}$$

$$Power_{Max} = FF \times J_{sc} V_{oc}$$

V_{oc} = Open circuit voltage
 V_{mp} = Max power voltage
 J_{sc} = Short circuit current
 J_{mp} = Max power current

Variables

h = Planck's constant = $4.1 \times 10^{-15} \text{ eV} \cdot \text{s}$

c = speed of light = $3.0 \times 10^8 \text{ m/s}$

k_B = Boltzmann's constant = $1.38 \times 10^{-23} \text{ m}^2 \text{ kg s}^{-2} \text{ K}^{-1}$

$q = e$ = elementary charge = $1.6 \times 10^{-19} \text{ C}$

B = Intensity- in W/m^2

λ = wavelength- in nm (can also be in m)

E = Energy- in eV (can also be in J)

I = Current (mA)

J = Current density (mA/cm^2)

J_0 = Dark saturation current density (mA/cm^2)

J_{sc} = Short-circuit current density (mA/cm^2)

μ = efficiency (in %)

$\Delta\mu$ = Chemical potential

F_s = Solid angle of emission from the Sun to Earth = 6×10^{-5}

F_e = Solid angle emission of Earth

F_a = Solid angle of emission from solar cell (normally π , but can vary)

Ideal Diode Equation

- Lets integrate the entire J_{net} equation over all energies:

$$J_{net} = q \int_{E_G}^{\infty} (1 - R(E)) \times (b_{sun}(E) + b_{amb}(E) - b_{emit}(E, \Delta\mu))$$

$$J_{net} = J_{sc} - J_0 \left[\exp\left(\frac{qV}{kT}\right) - 1 \right]$$

where J_0 is defined as:

Important point of J_0

This is a function of temperature

$$J_0 = \frac{1}{\eta} q F_a \frac{4kT}{h^3 c^2} \times (E_g^2 + 2kT E_g + (kT)^2) \times \exp\left(\frac{-E_g}{kT}\right)$$

Emission angle (π if you have a perfect back reflector)

Collection efficiency (includes reflection)

Maximum efficiency- Shockley-Queisser

- If we actually integrate the current over all energies/wavelengths and assume 100% absorption and 0% reflection, we get the Shockley-Queisser limit.

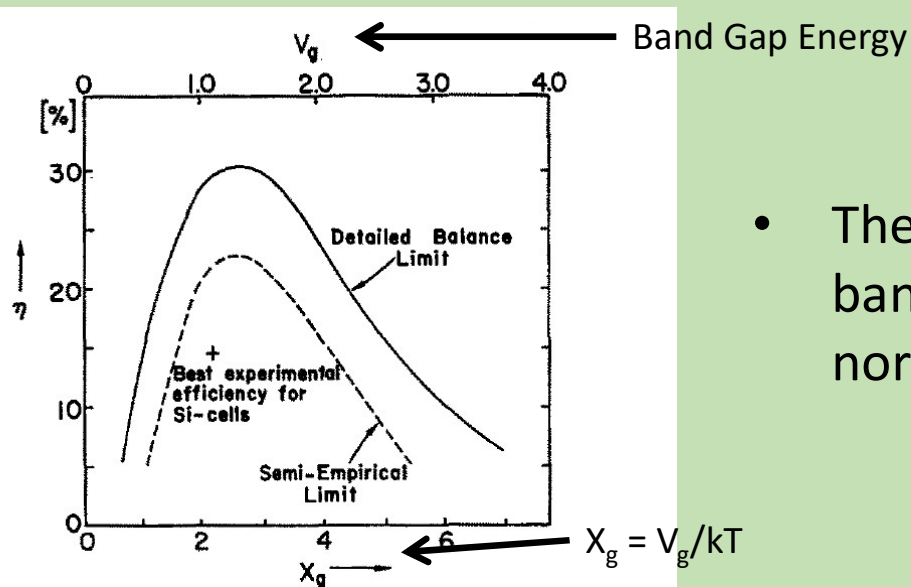


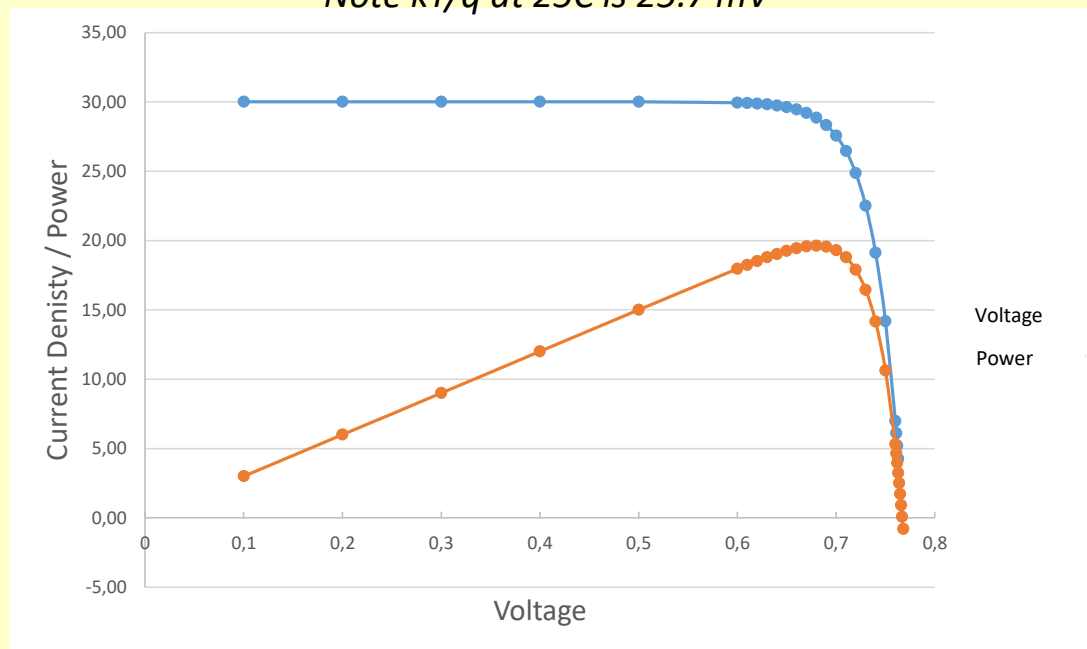
FIG. 1. Comparison of the "semiempirical limit" of efficiency of solar cells with the "detailed balance limit," derived in this paper. + represents the "best experiment efficiency to date" for silicon cells. (See footnote 6.)

- The maximum efficiency for a single band-gap photoabsorber under normal sunlight is **33%**

Applying diode equation

- If I have a solar cell with a dark saturation current (J_0) of 1×10^{-11} mA/cm² and a short circuit current (J_{sc}) of 30 mA/cm², what is my maximum power at a temperature of 25 °C ? or more simply, what is the power density at 0.5V?

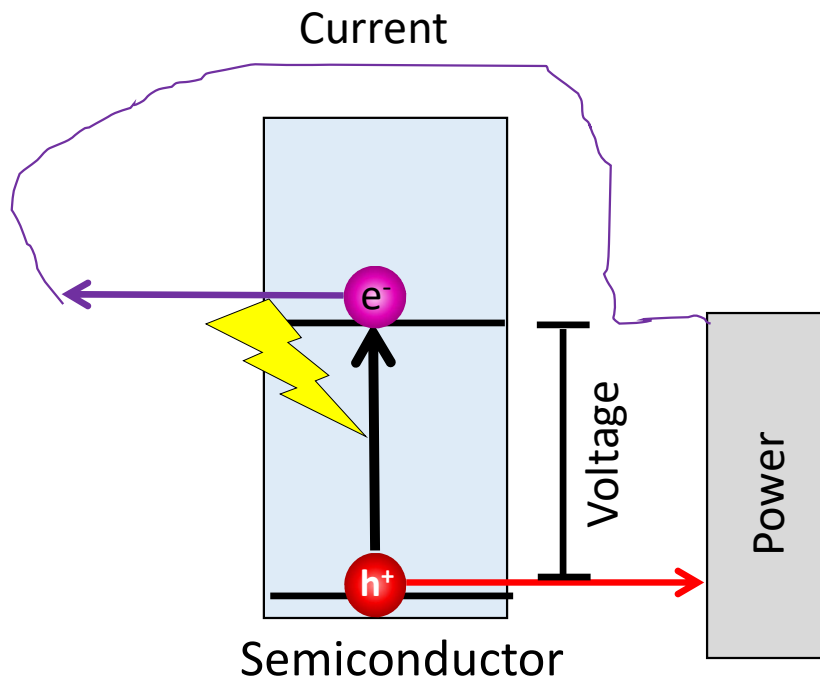
Note kT/q at 25C is 25.7 mV



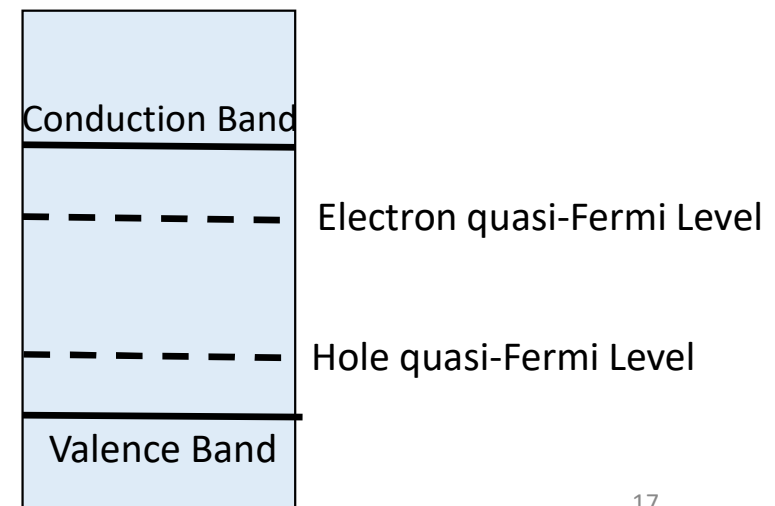
Answer = at 0.68V power is 19.6 mW/cm²

Solar cells – more detailed description

- From a first order theory we should be able to get power according to the voltage and current

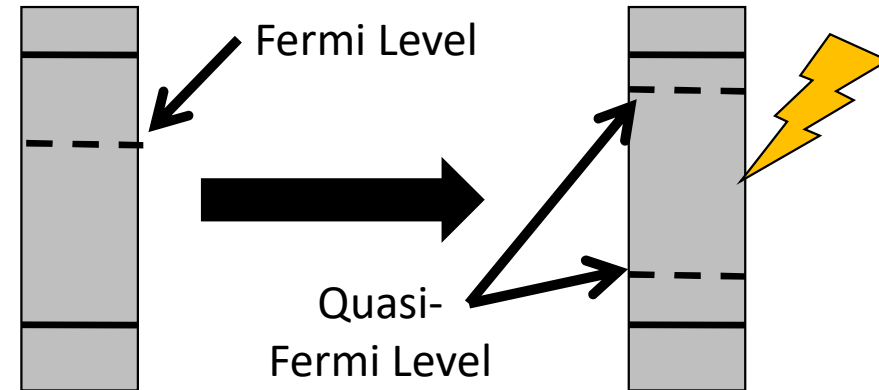


- From a more in-depth approach it is actually the splitting of our Fermi level that gives us photovoltage.



Physics of a Photovoltage

- During irradiation we add electron-hole pairs (add n and p)
- This provides a splitting of the Fermi level



Conduction Band: $E_{f,e-} = E_c + k_b T \ln \left(\frac{n}{N_c} \right)$

Valence Band: $E_{f,h+} = E_v - k_b T \ln \left(\frac{p}{N_v} \right)$

Photovoltage: $qV_{Phot} = E_{f,e-} - E_{f,h+}$

$$N_c = 2 \left(\frac{m_c^* k_B T}{2\pi \hbar^2} \right)^{3/2}$$

m_c - effective mass of electrons

$$N_v = 2 \left(\frac{m_v^* k_B T}{2\pi \hbar^2} \right)^{3/2}$$

m_v - effective mass of holes

Analysis of Photovoltage

- The photovoltage is sometimes denoted as a difference in chemical potential ($\Delta\mu$)
- By rearranging the photovoltage equation we get the following

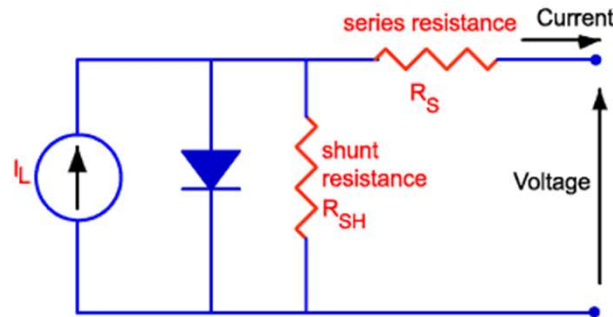
$$qV_{Photo} = \Delta\mu = E_g + k_b T \ln \left(\frac{pn}{N_v N_c} \right)$$

This is a negative term since $\ln < 1$ is negative

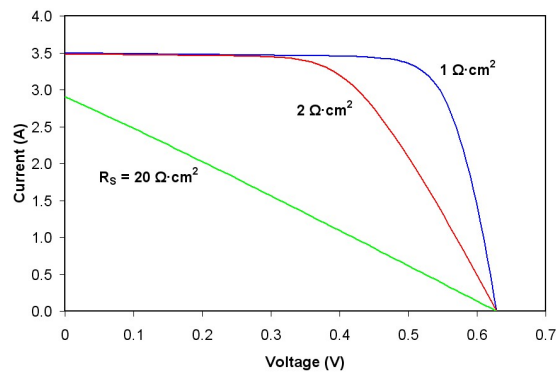
- N_v and N_c relate to band gap (intrinsic property) and effective mass (material specific).

Practical Losses -Shunt & Series Losses

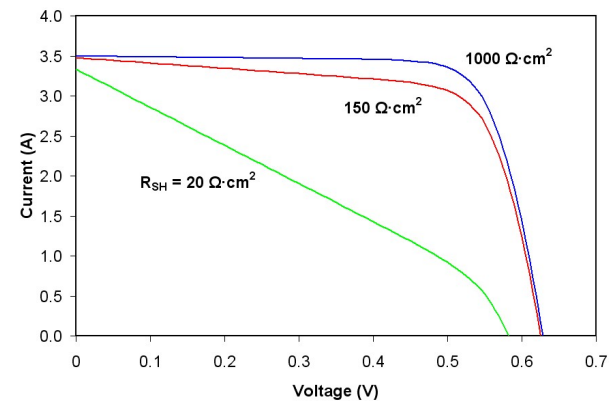
- The circuit for a shunt and series loss solar cell looks as followed:



Effects of Series Losses i.e. ohmic losses



Effects of Shunt Losses-i.e. short circuit



Diode Equation + Practical Losses

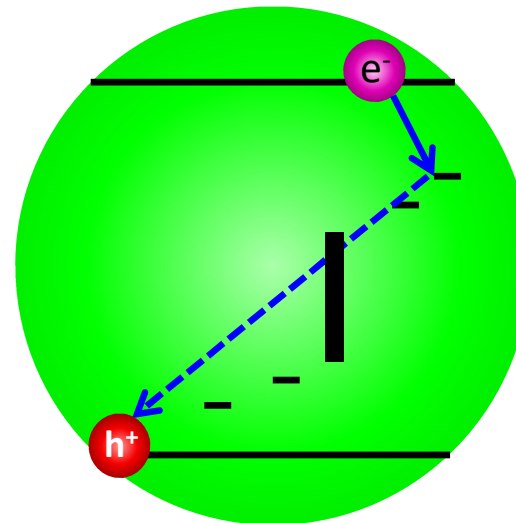
$$J_{net} = J_{sc} - J_0 \left[\exp \left(\frac{qV}{kT} \right) - 1 \right]$$

- **Series Resistance (R_s)** are losses due to any ohmic resistance in the system. We want low series resistance
 - This can be external (resistance in wire to solar cell) or internal (resistance within the semiconductor)
- **Shunt Resistance (R_{sh})** are losses due to internal short circuiting of the cell. Thus we want high shunt resistance
- Including shunt and series into our diode equation we get:

$$J_{net} = J_{sc} - J_0 \left[\exp \left(\frac{q(V + J_{net}R_s)}{kT} \right) - 1 \right] + \frac{q(V + J_{net}R_s)}{R_{sh}}$$

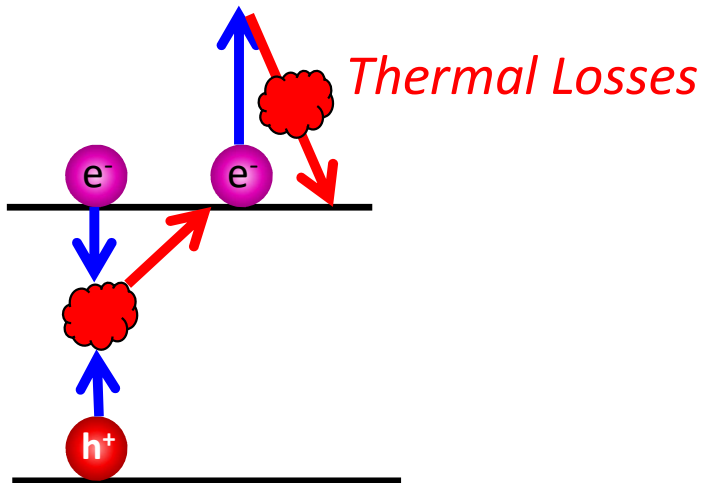
Non-radiative Recombination - Qualitative

- If we have defect sites in our solar cell, electrons and holes will recombine at these sites giving off heat.
- More precisely, the electron-hole recombination will emit photons, but just at too small of wavelengths to be reabsorbed by the semiconductor.
- This is also known as Shockley-Reed-Hall (SRH) recombination.



Auger Recombination (also non-radiative)

- If an electron and hole recombine, they can transfer their energy to a 2nd electron in the conduction band
- This 2nd electron goes up and energy, and then comes back down.



- When the 2nd electron comes back down, its energy is lost as non-radiative recombination.
- For this to take place, there needs to be a lot of electrons in the conduction band.

Recombination Losses in General

- *Shockley-Hall-Reed recombination (SRH)*- is always a bad thing thus this must be avoided.
 - High purity materials and good engineering can almost completely eliminate these losses
- *Radiative recombination (RR)*- This is black-body emissions that occur when deriving the Shockley-Queisser Equation
 - Note these radiated photons can get reabsorbed by the solar cell.
- *Auger recombination (AR)*- This is a minor loss
 - AR only occurs if there are lots of electron-hole pairs.

An analysis of efficiency

- Let's look at our diode equation and see where the losses are from a fundamental standpoint.

$$J_{net} = J_{sc} - J_0 \left[\exp \left(\frac{qV}{mkT} \right) - 1 \right]$$


← m = non-ideality factor (defects, etc.)
 $m=1$ for ideal case

$$V = \frac{mkT}{q} \ln \left(\frac{J_{sc} - J_{net}}{J_0} + 1 \right) \quad \longrightarrow \quad V_{oc} = \frac{mkT}{q} \ln \left(\frac{J_{sc}}{J_0} + 1 \right)$$

Does increasing the temperature increase the open circuit voltage?

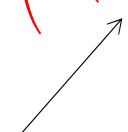
Finding all the efficiency losses

- By isolating V_{OC} , we can expand the J_0 term, simplify and more easily analyze our losses.


$$V_{OC} = \frac{kT}{q} \ln \left(\frac{j_{sc}}{j_0} + 1 \right)$$


$$V_{OC,Max} \approx \frac{E_G}{q} \left(1 - \frac{T}{T_S} \right) + \frac{kT}{q} \ln \left(\frac{T_S}{T} \right) - \frac{kT}{q} \left(\ln \left(\frac{\Omega_{Device}}{\Omega_{Sun} * \tau} \right) + \ln (4n_r^2) + \ln \left(\frac{R_{rad} + R_{non}}{R_{rad}} \right) \right)$$


Entropy Terms



Angle of emission
vs. absorption



Reflection losses



Effectively combination
of 'm' and 'η'

- The above equation lets us analyze where are our losses coming from

Finding all the efficiency losses

- Putting all the loss and gain terms together and simplifying yields:

$$V_{OC,Max} = \underbrace{\frac{E_G}{q} \left(1 - \frac{T}{T_S}\right) + \frac{kT}{q} \ln\left(\frac{T_S}{T}\right)}_{\text{Blackbody radiation losses}} - \underbrace{\frac{kT}{q} \left(\ln\left(\frac{\Omega_{Device}}{\Omega_{Sun} * \tau}\right) + \ln(4n_r^2) + \ln\left(\frac{R_{rad} + R_{non}}{R_{rad}}\right) \right)}_{\text{Entropy Terms}}$$

- Determine how much loss each term contributes.
- Determine the maximum efficiency for the following materials:
 - Si ($E_g = 1.1$ eV, average $n_r = 3.4$)
 - GaAs ($E_g = 1.4$ eV, average $n_r = 3.3$)
 - $\text{PbCH}_3\text{NH}_3\text{I}_3$ Perovskite ($E_g = 1.5$ eV, average $n_r = 2.5$)

-Assume $\Omega_{Device} = \pi$, no non-radiative recombination, and a no light concentration (i.e $\tau = 1$) . $\Omega_{Sun} = 6 \times 10^{-5}$

Finding all the efficiency losses

- Putting all the loss and gain terms together and simplifying yields:

$$V_{OC,Max} = \frac{E_G}{q} \left(1 - \frac{T}{T_S} \right) + \frac{kT}{q} \ln \left(\frac{T_S}{T} \right) - \frac{kT}{q} \left(\ln \left(\frac{\Omega_{Device}}{\Omega_{Sun} * \tau} \right) + \ln (4n_r^2) + \ln \left(\frac{R_{rad} + R_{non}}{R_{rad}} \right) \right)$$

Entropy Terms

- If all terms are highly optimized the $V_{OC, Max}$ is typically about 300 mV less than the band gap (i.e. E_G)
- In theory the entropy terms can be engineered to almost zero, but this may create an impractical design from a manufacturing or economic perspective.

<i>Best Experimental $V_{OC, max}$</i>		
Material	E_G	$V_{OC, max}$
Si	1.1	0.740
GaAs	1.4	1.12
PbCH ₃ NH ₃ I ₃ (Perovskite)	1.55	~1.2

Removing non-radiative recombination

- Understanding all the terms.

$$V_{OC,Max} = \frac{E_G}{e} \left(1 - \frac{T}{T_S} \right) + \frac{kT}{e} \ln \left(\frac{T_S}{T} \right) - \frac{kT}{e} \left(\ln \left(\frac{\Omega_{Device}}{\Omega_{Sun} * \tau} \right) + \ln (4n_r^2) + \ln \left(\frac{R_{rad} + R_{non}}{R_{rad}} \right) \right)$$

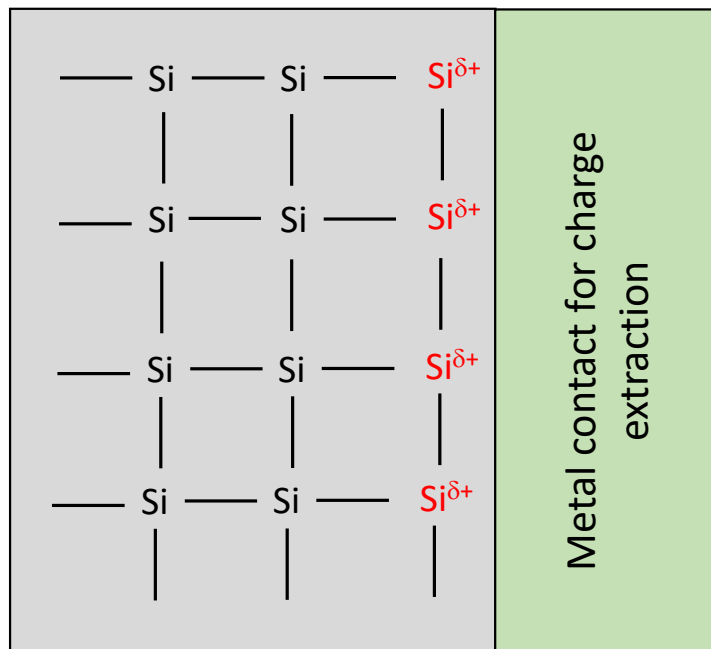


How can we
effectively limit this
term?

- Have a more pure, and well ordered semiconductor (don't have junk in your silicon)

Other non-radiative recombination sites

- Surface defects are the other major area for non-radiative recombination.
- These results from incomplete bonds between surfaces.



Si Wafer

- This is probably the biggest fixable loss in solar cells.
- The best way to mitigate these is to create an insulating layer at the surface.
- There is a lot of technology in trying to resolve this issue.

Finding all the efficiency losses

Entropy Terms

$$V_{OC,Max} = \frac{E_G}{q} \left(1 - \frac{T}{T_S} \right) + \frac{kT}{q} \ln \left(\frac{T_S}{T} \right) - \frac{kT}{q} \left(\ln \left(\frac{\Omega_{Device}}{\Omega_{Sun} * \tau} \right) + \ln \left(4n_r^2 \right) + \ln \left(\frac{R_{rad} + R_{non}}{R_{rad}} \right) \right)$$

- Is there any tricks to mitigate the first two entropy loss terms.
- Obviously we can't beat the 1st law of thermodynamics, but we can manipulate entropy to our advantage.

Trying to 'Beat the system'

- Understanding all the terms.

$$V_{OC,Max} = \frac{E_G}{e} \left(1 - \frac{T}{T_S} \right) + \frac{kT}{e} \ln \left(\frac{T_S}{T} \right) - \frac{kT}{e} \left(\text{Ln} \left(\frac{\Omega_{Device}}{\Omega_{Sun} * \tau} \right) + \text{Ln} (4n_r^2) + \text{Ln} \left(\frac{R_{rad} + R_{non}}{R_{rad}} \right) \right)$$



How can we
effectively limit this
term?

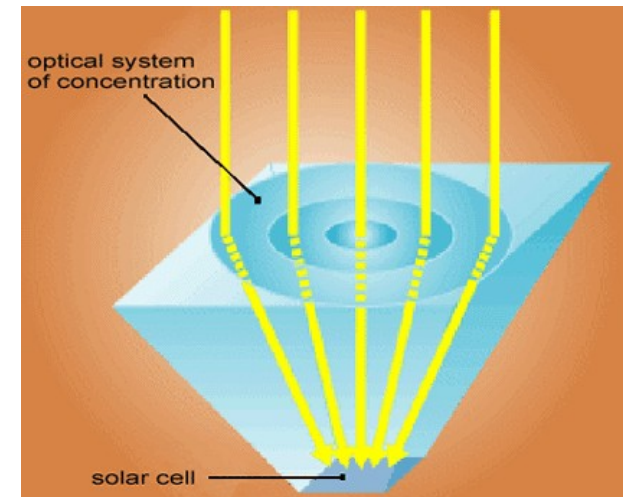
Concentrator cells

- Concentrator cells simply are mirrors that concentrate the light onto a solar cell.
- Concentrators are nice for 2 reasons:
 - Increase efficiency slightly.
 - You lower the solar cell cost.

$$V_{OC} = \frac{mkT}{q} \ln \left(\frac{j_{sc}}{j_0} + 1 \right)$$

$$V_{increase} = \frac{mk}{q} \ln \left(\frac{i_{con.}}{i_{uncon.}} \right)$$

Assume $m=1$ for ideal case



Concentrator cells



- If the solar cell cost is high (i.e. use rare or expensive materials, this approach is very beneficial.)
- These cells work good in direct sunlight, not indirect or diffuse sunlight, thus they need to track the sunlight
- Increase in temperature can be a major issue (*Why?*) and cooling systems are needed on these devices.
- Thus the economic viability of these cells is very geography dependent.
- Concentrators range from 10x concentration up to 1,000x.

Trying to 'Beat the system'

- Understanding all the terms.

$$V_{OC,Max} = \frac{E_G}{q} \left(1 - \frac{T}{T_S} \right) + \frac{kT}{q} \ln \left(\frac{T_S}{T} \right) - \frac{kT}{q} \left(\ln \left(\frac{\Omega_{Device}}{\Omega_{Sun} * \tau} \right) + \textcolor{red}{Ln(4n_r^2)} + \ln \left(\frac{R_{rad}^{net} + R_{non}}{R_{rad}^{net}} \right) \right)$$

How can we effectively limit this term?

Mitigating Light Reflection

$$r = \frac{(n_o - n_s)^2}{(n_o + n_s)^2}$$

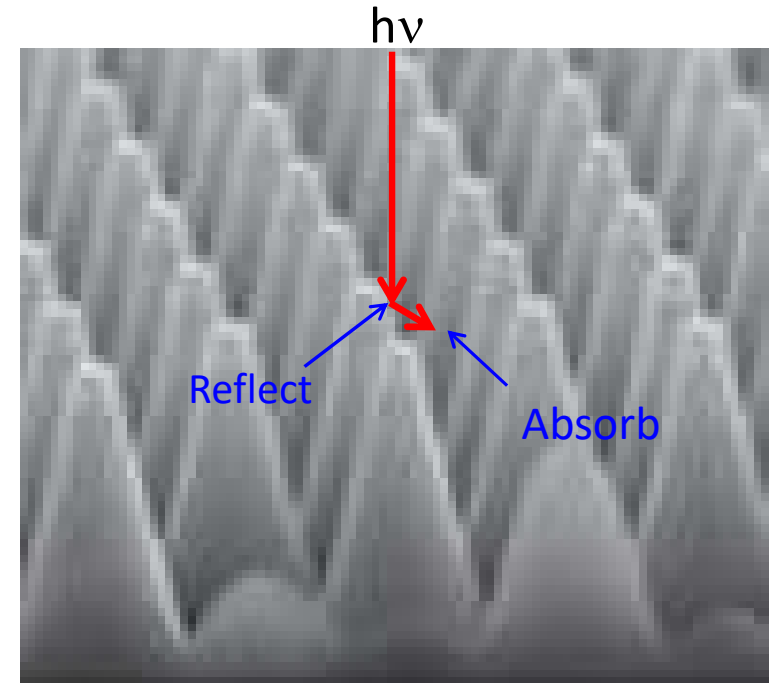
Air Substrate
↓ ↓

- Strategies to reduce r

- Nanotexturing the surface.
- This allows the light to have multiple chances to get absorbed.

- Basically $r_{eff} = r^n$ ← $n = \# \text{ of reflections}$

- If the probability of reflection is 20%, and the light bounces off the semiconductor 3 times, the effective reflectivity is 0.8%.

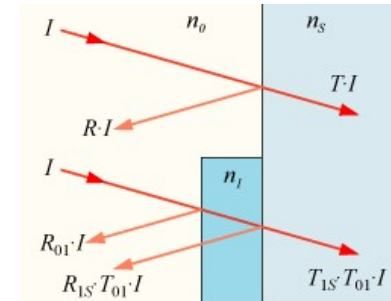


Mitigating light reflection

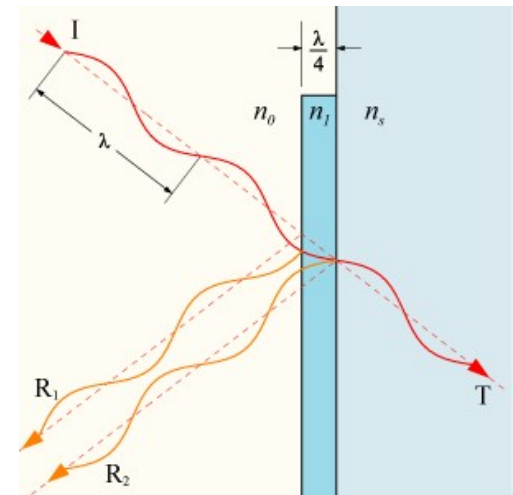
- Antireflective coating- Approach #1
 - By having a coating with an intermediate n_r , it is possible to decrease reflection losses.
 - The optimum index of refraction should be:

$$n_1 = \sqrt{n_0 n_s}$$

Remember: $r = \frac{(n_o - n_s)^2}{(n_o + n_s)^2}$



- Antireflective coating- Approach #2
 - If the anti-reflective layer is $\frac{1}{4}$ the wavelength of incoming light, the reflected light will destructively interfere.
 - This is a limited approach since solar irradiation is not a single wavelength, but a range of wavelengths.



p-n Junctions

(may be done in Week 3)

Doping a Semiconductor

i.e.
Changing the Fermi level

Periodic Table of Elements



1 2 3 4 5 6 7 8 9 10										p-type	1 n-type 15 16 17 18																																																												
1 H Hydrogen 1.00794		4 Be Beryllium 9.012182		11 Na Sodium 22.98976928		12 Mg Magnesium 24.3050		19 K Potassium 39.0983		20 Ca Calcium 40.078		21 Sc Scandium 44.955912		22 Ti Titanium 47.887		23 V Vanadium 50.9415		24 Cr Chromium 51.9961		25 Mn Manganese 54.938045		26 Fe Iron 55.845		27 Co Cobalt 58.933195		28 Ni Nickel 58.6934		29 Cu Copper 63.546		30 Zn Zinc 65.38		31 Ga Gallium 69.723		32 Ge Germanium 72.64		33 As Arsenic 74.9216		34 Se Selenium 78.96		35 Br Bromine 79.904		36 Kr Krypton 83.798																													
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For elements with no stable isotopes, the mass number of the isotope with the longest half-life is in parentheses.

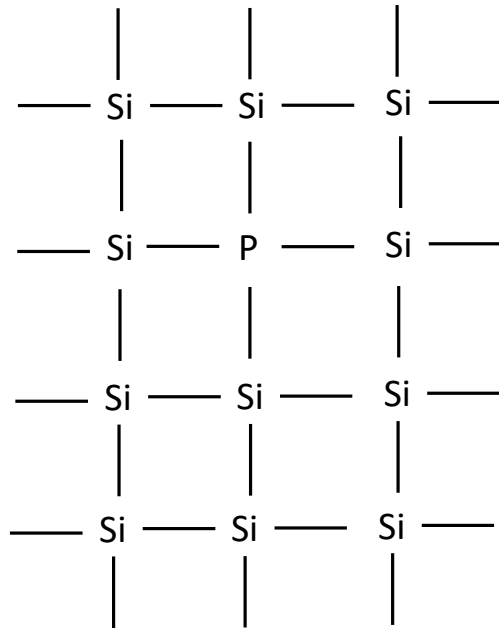
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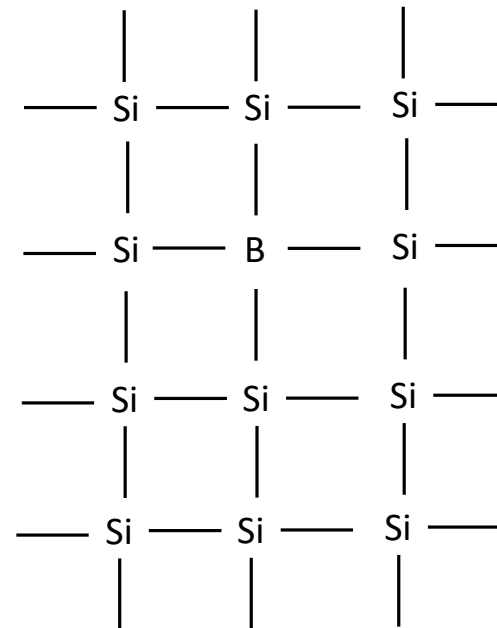
57 La Lanthanum 138.9047	58 Ce Cerium 140.116	59 Pr Praseodymium 140.90768	60 Nd Neodymium 144.242	61 Pm Promethium (145)	62 Sm Samarium 150.36	63 Eu Europium 151.964	64 Gd Gadolinium 157.25	65 Tb Terbium 158.92535	66 Dy Dysprosium 162.500	67 Ho Holmium 164.93032	68 Er Erbium 167.259	69 Tm Thulium 168.93421	70 Yb Ytterbium 173.054	71 Lu Lutetium 174.9668
89 Ac Actinium (227)	90 Th Thorium 232.03806	91 Pa Protactinium 231.03688	92 U Uranium 238.02891	93 Np Neptunium (237)	94 Pu Plutonium (244)	95 Am Americium (243)	96 Cm Curium (247)	97 Bk Berkelium (247)	98 Cf Californium (251)	99 Es Einsteinium (252)	100 Fm Fermium (257)	101 Md Mendelevium (258)	102 No Nobelium (259)	103 Lr Lawrencium (262)

How to get an n-type or p-type material

- Here are the most common ways to make Si n-type or p-type.



n-type

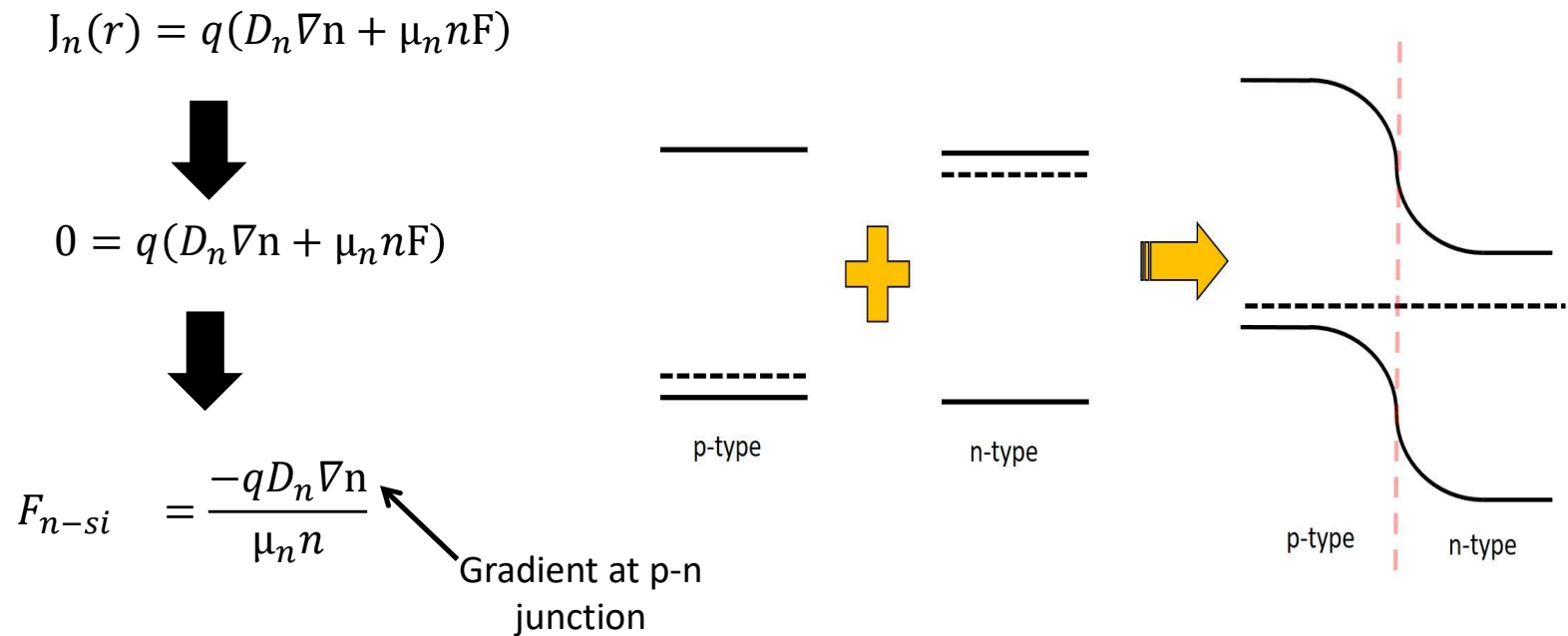


p-type

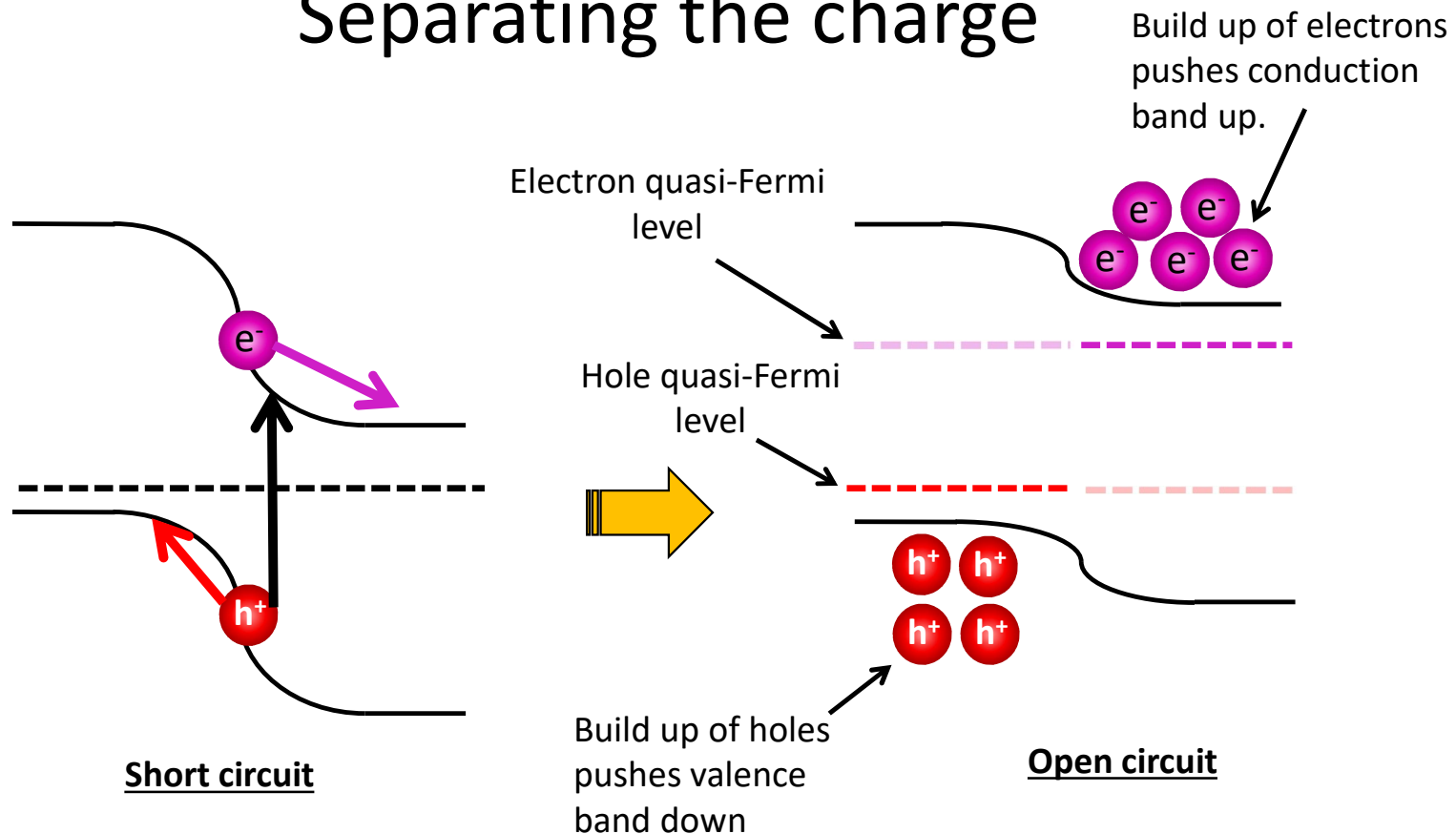
- Here are the most common ways to make Si n-type or p-type.

Separating the charge

- Creating a p-n junction allows us to create a built in electrochemical bias.
- At the interface charge transfers between n-side and p-side due to diffusion until it builds enough potential to make current = 0.

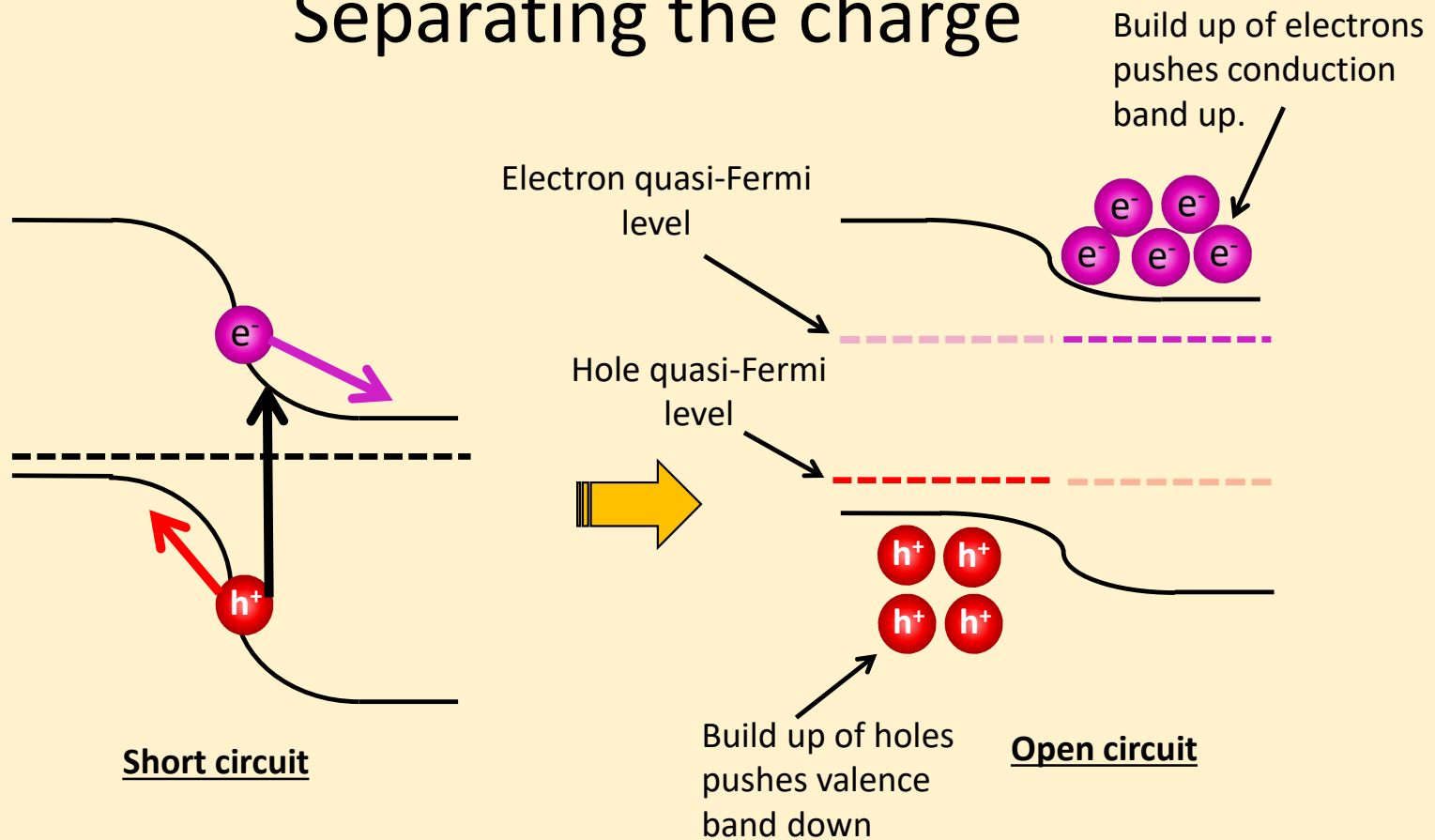


Separating the charge



- Just because an electron is in the conduction band, doesn't mean that this is the chemical potential of the electron.
- The chemical potential of the electron is that of the quasi Fermi-Level

Separating the charge



- Will the band-bending thickness be equally between the p and n side.

Doping Profiles

- The doping is inversely proportional to the doping density.

$$V_{p-type} = V_{Bias} \times \frac{N_D}{N_D + N_A}$$

$$V_{n-type} = V_{Bias} \times \frac{N_A}{N_D + N_A}$$

N_A = Acceptor (p-type) density

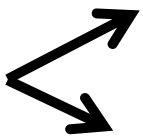
N_D = Donor (n-type) density

- V_{bias} is the potential difference in Fermi levels between the n-type and p-type semiconductor.
- For more detailed description of these equations see [Malizia, et al, JMC-A, 2014](#).

Doping Profiles

- Basically the high dopant density material has a stronger pull than the lower doped material.
- By using Poisson's equation to distribute the charge, we can determine the depletion width.

Depletion width
(band bending
thickness)


$$x_p = \left(\frac{N_D}{N_A} \frac{2\epsilon\epsilon_0 V_{bias}}{q(N_D + N_A)} \right)^{1/2}$$
$$x_n = \left(\frac{N_A}{N_D} \frac{2\epsilon\epsilon_0 V_{bias}}{q(N_D + N_A)} \right)^{1/2}$$

ϵ = permittivity of semiconductor

ϵ_0 = permittivity in vacuum

V_{bias} = Total band-bending voltage (difference in p-n Fermi levels)

q = elementary charge

Concept Check

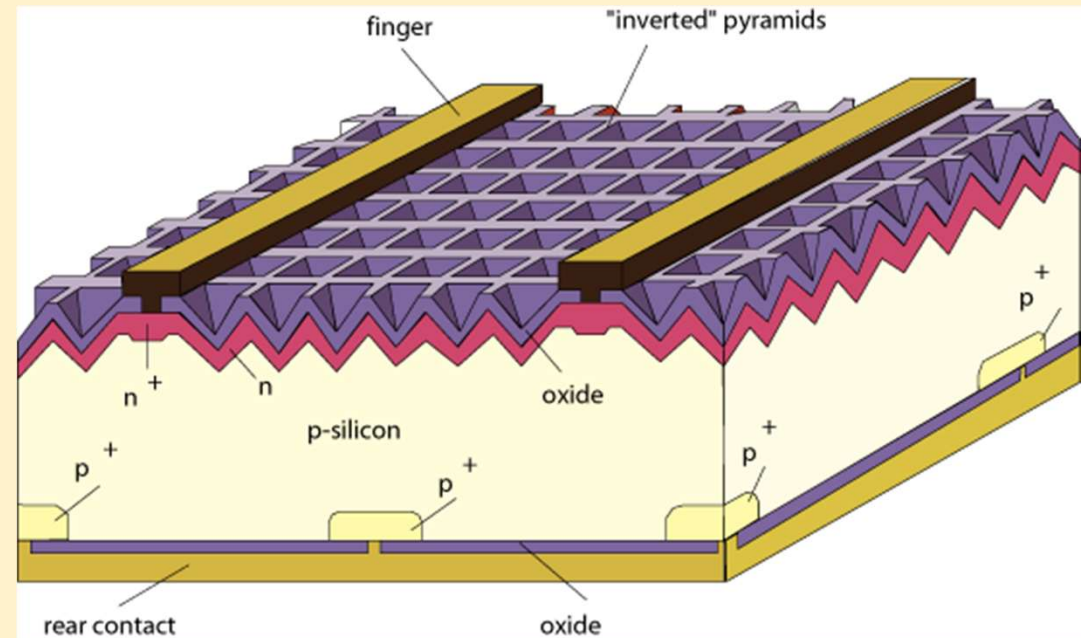


In a p-n junction solar cell, a p-type side has a dopant density of 10^{16} and an n-type side has a dopant density of 10^{20} . This means:

- a) The p-type has a larger voltage drop across it and a longer depletion layer.
- b) The p-type has a larger voltage drop across it and a shorter depletion layer.
- c) The n-type has a larger voltage drop across it and a longer depletion layer.
- d) The p-type has a larger voltage drop across it and a shorter depletion layer.

State of the art - 2013

- Creating small point contacts allows for minimal surface recombination.
- Doping both sides prevents charge carriers from going to the wrong contact.
- Creating small point contacts allows for minimal surface recombination.
- This approach gave a record efficiency of 24.7%.
- What is the biggest failure of this device?



State of the art - Current

- Panasonic decided to put both the electron and hole contact on the same side.
- This eliminated light shading by the electrical contact fingers and allowed complete surface passivation on one side.
- Amorphous Si was used as back contacts because they minimize recombination losses.
- This device reached a record 26.7% efficiency.
- It is still surprising that having both the p and n junction near each other gives such good efficiency.

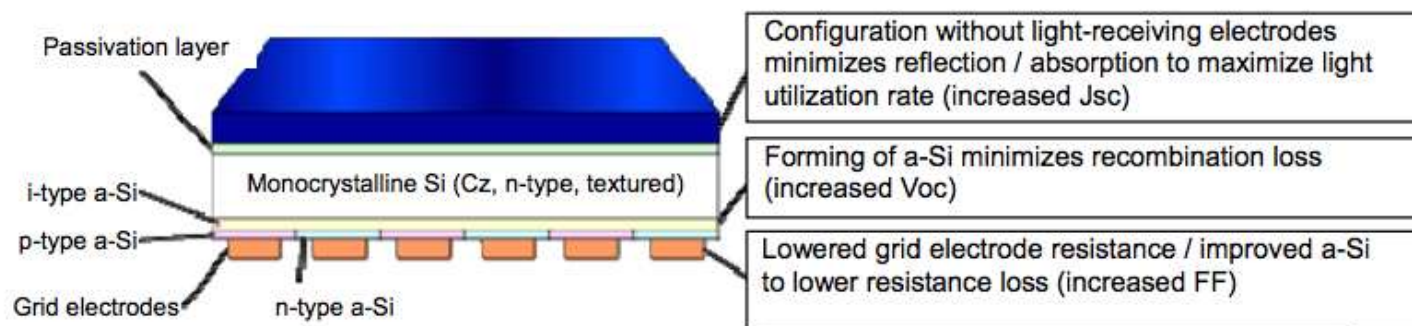


Image from [Natural Group](#)

Lecture - Learning Objectives

At the end of this lecture you should:

- Understand the detailed balance for solar cells, and why maximum efficiency for a single photoabsorber is 33%
- Be able to analyze the basic principles of photovoltage and factors that can effect it
- Understand how p-n junctions work and their relation to solar cells.

Exercises

- Currently the best crystalline Se solar cells have an open circuit voltage of 1.2 V at 10 times solar concentration. What is their thermodynamic maximum voltage they can achieve? Is it worth investing more research money into this material?
- If I use TiN as an antireflection layer on Silicon, how much will I reduce the reflection by (at a wavelength of 590 nm)?
- At 8 AM my silicon solar cell has a short circuit current of 100 A and an open circuit voltage of 0.6 V and a fill factor of 80%. What is its maximum power? Now At 12 PM there is 4 times more light (but the same temperature, and same fill factor). In theory, how much will my solar cell produce at this time?